**Bajaj College of Science, Wardha (Autonomous)**

**Department of Mathematics**

**M.Sc. Syllabus**

**Metrtic 1.1.3 Details of courses offered by the institution that focus on employability/entrepreneurship/skill development during the year**

**Syllabus PG (2023-24)**

**M. Sc. Mathematics**

**Semester-I**

**DSC- 1 (Algebra )**

**Unit I:** Permutation Group. Normal subgroups, Quotient groups Dihedral group. Commutator group. Isomorphism Theorems. Automorphisms. Characteristic subgroup. Conjugacy and G-Sets, -Cyclic Decomposition

**Unit II:** Normal Series. Solvable groups. Nilpotent groups. Cyclic decomposition of permutation group. Alternating groups. Simplicity of An.

**Unit III:** Direct product, semi-direct product of groups, infinitely generated abelian groups -Invariants of a finite abelian group, Sylows theorems. Groups of order and pq.

**Unit IV:** Ideals and Homomorphisms. Sum and direct sum of ideals. Maximal and prime ideals. Nilpotent and Nil ideals. Modules. Submodules. Direct sums. R-homomorphisms and quotient modules. Completely reducible modules. Free modules

**Text Book:**

Basic Abstract Algebra: Bhattacharya, Jain, and Nagpal, Second Edition,

Cambridge University Press.

**Reference Books:**

1. Topics in Algebra, I. N. Herstein, Second Edition, John Wiley.

2. Abstract Algebra: David S.Dummit and Richard M. Foote, John Wiley.

**DSC-2 (Topology)**

**Unit I:**Countable and Uncountable sets. Examples and related Theorems. Cardinal Numbers and related Theorems. Topological Spaces and Examples.

**Unit II:**Open sets and Limit points, Derived Sets. Closed sets and closure operators. Interior, Exterior and boundary operators. Neighbourhoods, bases and relative topologies.

**Unit III:**Connected sets and components. Compact and countably compact spaces. Continuous functions and homeomorphisms, Arc wise connectivity.

**Unit IV:** and -spaces, -spaces and sequences. Axioms of countability. Separability. Regular and normal spaces.

**Text Book:**

Foundations of General Topology: W.J. Pervin, Academic press, 1964.

**Reference Books:**

1. Topology: J.R. Munkres, (second edition), Prentice Hall of India, 2002.

2. Introduction to Topology and Modern Analysis: G.F. Simmons, Mc Graw Hill 1963.

3. General Topology: J.L. Kelley, Van Nostrand, 1995.

4. Introduction to general Topology: K.D. Joshi, Wiley Eastern Ltd. 1983

**DSC-3 (Ordinary Differential Equations)**

**Unit I:**Linear Equations with variable coefficients: Initial value problems for the homogeneous equations. Solutions of the homogeneous equations, The Wronskian and linear independence, Reduction of the order of a homogeneous equation, The non-homogenous equations, Homogeneous equations with analytic coefficients, The Legendre equations.

**Unit - II:**Linear Equations with regular singular points: The Euler equations, Second order equations with regular singular points, The Bessel equation, Regular singular points at infinity.

**Unit III:**Existence and uniqueness of solutions to first order equations: The method of successive approximations, The Lipschitz condition of the successive approximation. Convergence of the successive approximation, Non-local existence of solutions, Approximations to solutions and uniqueness of solutions.

**Unit IV:**Existence and Uniqueness of Solutions to System of first order ordinary differential equations: An example- Central forces and planetary motion, Some special equations, Systems as vector equations , Existence and uniqueness of solutions to systems, Existence and uniqueness for linear systems, Green's function, Sturm Liouville theory.

**Text Book:**

1. E.A.Coddington: An introduction to ordinary differential equations (2012),Prentice Hall of India Pvt.Ltd. New Delhi.

2. G. Birkoff and G.G.Rota: Ordinary Differential equations, John Willey and Sons

3. Mark Pinsky: Partial differential equations and boundary-value problems with applications, AMS, 3rd edition(2011).

**Reference books**:

1. G.F. Simmons Differential Equations with Applications and Historical note, MeGraw Hill, Inc. New York. (1972)

2. E.A. Coddington and Levinson: Theory of ODE McGraw Hill, New York(1955)

3. E.D. Rainvills:Elementary differential equations, The Macmillan company, New York. (1964)

**DSC 4 –Practical**

**(Algebra, Topology and Ordinary Differential Equations)**

**List of Practical:**

1) Representation of the permutations as a product of disjoint cycles

2) Determination of order of an element and order of a group

3) Determination of composition series for the group.

4) Investigation of simple groups.

5) Determination of right and left ideals of the ring.

6) Determination of maximal and prime ideals.

7) Determination of kernel of homomorphism of a ring.

8) Finding solution of Differential Equation using method of Reduction of order.

9) Finding solution of Linear Differential Equation with regular singular points.

10) Derivation of Recurrence Relation on Bessel Function.

11) Determination of approximate solution of Differential Equation using successive Approximations.

12) Examination of Lipschitz Conditions and determination of Lipschitz constant.

**DSE-1 (Integral Equations)**

**Unit 1:**Preliminary concepts of integral equations. Some problems which give rise to integral equations. Conversion of ordinary differential equations into integral equations. Classification of linear integral equations. Integro-differential equations.

**Unit 2:**Fredholm equations. Degenerate kernels. Hermitian and symmetric kernels. The Hilbert- Schmidt theorem. Hermitization and symmetrization of kernels. Solutions of integral equations with Green’s function type kernels.

**Unit 3:**Types of Voltera equations. Resolvent kernel of Voltera equations, Convolution type kernels. Some miscellaneous types of Voltera equations. Non-linear Voltera equations. Fourier integral equations. Laplace integral equations.

**Unit 4:**Hilbert transform. Finite Hilbert transforms. Miscellaneous integral transforms. Approximate methods of solutions for linear integral equations. Approximate evaluation of Eigen values and Eigen functions.

**Text Book:**

Integral Equations: A short course: L. G. Chambers: International text book company Ltd, 1976.

**Reference books:**

1. Integral equations by Shanti Swaroop, Shiv Raj Singh

2. Linear integral equation, Theory and techniques, Academic press, New York 1971

3. R.P. Kanwal, Linear Integral Equation, Theory and Techniques, Academic Press,N.Y. (1971).

4. S.G. Mikhlin, Linear Integral Equations, Hindustan Book Agency, (1960).

5. A.M. Viazwaz, A First Course in Integral Equations, World Scientific (1997).

6. L.I.G. Chambers, Integral Equation: A Short Course, International Text Book Company Ltd. (1976).

7. Larry Andrews, Bhimsen Shiramoggo, Integral Transform for Engineers, Prentice Hall of India (2003).

8. Integral equations and boundary value problems by M. D. Raisinghania, S. Chand Publication

**Research Methodology (RM)**

**Module 1:** Research basics and perception of research:

**1.1** Definition, General and specific characteristics of research, types of research (basic, applied and patent oriented).

**1.2** Steps of Action (basic) research, objectives of basic research, characteristics of investigators.

**1.3** Scientific thinking- characters, steps in process of scientific thinking, Steps in problem identification, criteria for selecting problem, and sources of scientific problems.

**1.4** Review of literature- meaning, need, and objectives, structure of review of literature, sources of literature collection, Simple rules of structuring (writing) literature review.

**Module 2**: Statistical analysis**:**

**2.1**Errors in analysis. Classification of errors- systematic and random, additive, and proportional, absolute and relative. Accuracy and precision. Mean, median, average deviation and standard deviation.

**2.2**Significant figures and rules to determine significant figures. Calculations involving significant figures.

**2.3**Confidence limit, correlation coefficient and regression analysis. Comparison of methods: F-test and t-test. Rejection of data based on Q-test. Least squares method for deriving calibration graph.

**2.4**Application of Microsoft Excel in statistical analysis (statistical functions and spreadsheets in MS-Excel). Certified reference materials (CRMs). Numerical problems.

**Module 3:**Scientific Writing and Presentation:

**3.1**Scientific writing. Types of scientific publications- magazines, journals, reviews, news-letters, structure of scientific paper.

**3.2**Report Writing, different steps in report writing, types of reports, layout of research paper.

**3.3** Research indicators & Metrics: ImpactFactor, Cite Score, h-Index, i10-Index, Citation Index, references/bibliography, structuring the thesis, use of software in thesis writing.

**3.4** Intellectual Property Rights (IPR): Introduction to IPR (Patents, Trademarks, Geographical indicators, Copyright, and neighboring rights), concept and theories, kinds of IPR, Advantages and disadvantages of IPR.

**Module 4**: Use of tools / techniques for Research:

**4.1**Methods to search required information effectively, Various reference styles, Reference Management Software like Zotero/Mendeley,preparation of bibliography database.

**4.2** Software/tools: MS Word, MS Excel, Graph and chart preparation, MS Power Point, OriginLab (For plotting graph).

**4.3** Research ethics, Academic integrity, Plagiarism, types, detection of plagiarism using software.

**Reference/Books:**

1. Shanti Mishra, &Alok, S. (2011). Handbook of Research Methodology: A Compendium for Scholars & Researchers. Educreation Publishing.
2. Singh, Y. kumar. (2006). Fundamentals of Research Methodology and Statistics. New Age International Publishers.
3. Walliman, N. (2010). Research Methods The Basics. Routledge Taylor and Francis Group.
4. Research Methodology- C. R. Kothari
5. Best and Kahn, Research Methodology, PHI Limited
6. Design of Experience: Statistical Principles of Research Design and Analysis, by Robert O. Kuehl Brooks/cole.
7. Patrick Carey, Katherine T. Pinard, Ann Shaffer, Mark Shellman, New Perspectives Microsoft Office 365 and Office 2019 Introductory, 2020.

**M.Sc. Sem-II**

**DSC-5 (Real Analysis)**

**Unit I:**Uniform convergence. Uniform convergence and continuity. Uniform convergence and integration. Uniform convergence and differentiation. Equicontinuous families of functions. The Stone-Weierstrass theorem.

**Unit II:**Differentiation. The Contraction Principle. The Inverse Function Theorem. The Implicit Function Theorem. The Rank Theorem. Partitions of unity.

**Unit III:**Outer measure. Measurable sets and Lebesgue measure. A non-measurable set, Measurable functions, Littlewood’s three principles.

**Unit IV:**The Riemann integral. Lebesgue integral of a bounded function over a set of finite measure. Integral of a non-negative function. General Lebesgue integral. Convergence in measure. Differentiation of monotone functions. Functions of bounded variation. Differentiation of an integral.

**Text Books:**

1. Principles of Mathematical Analysis (Third Edition): Walter Rudin Mc GRAW – HILL Book Company.

2. Real Analysis, H.L. Royden, Third edition, Prentice Hall, 1988.

**Reference Books:**

1. Methods of Real Analysis: R. R. Goldberg, John Wiley.

2. Calculus of Several Variables: C Goffman, Harper and Row.

3. Measure theory and Integration, G. de Barra Wiley Eastern Limited, 1981.

4. An introduction to Measure & Integration, Inder K. Rana, Narosa Publishing House

**DSC-6 (Classical Mechanics)**

**Unit I:**Variational principle and Lagrange’s Equations: Hamilton’s principle, some techniques of the calculus of variations. Derivation of Lagrange’ s Equations from Hamilton’s Principle. Extension of principle to nonholonomic systems. Conservation theorems and symmetry properties.

**Unit II:**Legendre transformations and the Hamilton equations of motion, cyclic coordinates and conservation theorems, Routh’s equations, Derivation of Hamilton’s equations from a variational principle, the principle of least action.

**Unit III:** Canonical transformations: The equations of Canonical transformation, examples of canonical transformations. Symmetric approach to Canonical Transformation, Poisson’s bracket & other canonical invariants.

**Unit IV:**Equations of motion. Infinitesimal canonical transformations and conservation theorems in the Poisson bracket formulation, the angular momentum poisson bracket relations, Hamilton-Jacobi theory for Hamilton’s principle, and Hamilton-Jacobi theory for characteristic functions.

**Text Book:**

H. Goldstein, Classical Mechanics, Second edition, Narosa Publishing House, New Delhi

**References:**

1. T.M. Karade, G.S.Khadekar, Lectures on Advanced Mechanics, Sonu-Nilu publication

2. A.S.Ramsey Dynamics Part-II, the English Language Book Society and Cambridge University Press.

3. Gupta, Kumar and Sharma, Classical Mechanics

4. I.D. Landau and E.M. Lifchitz, Vol. I third edition, Perguman press, New Delhi

5. N. C. Rana &P .S. Joag ,Classical Mechanics ,Tata Mc Graw Hill

6. L. M. Katkar, Classical Mechanics(Mathematics), Shivaji University Kolhapur, 2007

**DSC-7 (Differential Geometry)**

**Unit I:**Definition of surface. Curves on a surface. Surfaces of revolution. Helicoids. Metric. Direction coefficients. Families of curves. Isometric correspondence. Intrinsic properties. Geodesics. Canonical geodesic equations.

**Unit II:**Normal property of geodesics. Existence theorems. Geodesic parallels. Geodesic curvature. Gauss Bonnet theorem. Gaussian curvature. Surfaces of constant curvature. Conformal mapping. Geodesic mapping.

**Unit III:**Second fundamental form. Principal curvatures. Lines of curvature. Developable. Developable associated with space curves. Developable associated with curves on surfaces. Minimal surfaces and ruled surfaces. Fundamental equations of Surface theory. Parallel surfaces.

**Unit IV:** Compact surfaces whose points are umbilics. Hilbert’s lemma. Compact surfaces of constant Gaussian or mean curvature. Complete surfaces. Characterisation of complete surfaces. Hilbert’s theorem. Conjugate points on geodesics. Intrinsically defined surfaces. Triangulation. Two dimensional Riemannian manifolds. Problem of metrization. Problem of continuation.

**Text Book:**

An introduction to Differential Geometry: T.J. Wilmore; Oxford University Press

**References:**

1. W. Klingenberg (Springer), A course in Differential Geometry

2. Geometry of curves and surfaces: do Carmo, Academic Press.

3. Weatherburn, C. Riemannian Geometry and Tensor Calculus

4. D. Somasundaram, Differential Geometry a first course, Narosa Publishing House,2008

**DSC-8 : Practical**

**(Real Analysis, Classical Mechanics and Differential Geometry)**

**List of Practical:**

1) Examination of convergence of Sequence and series of Functions.

2) Determination of Outer Measure of interval and sets.

3) Determination of Dini Derivatives of functions.

4) Determination of surface equation of Sphere.

5) Determination of curvatures of various surfaces.

6) Determination of Gaussian curvatures of various surfaces.

7) Determination of First Fundamental form of given surfaces.

8) Determination of Second Fundamental form of given surfaces.

9) Determination of shortest distance between two points in a plane.

10) Determination of minimum surface of revolution.

11) Finding the solution of Brachistochrone problem.

12) Determination of Hamilton’s equation and Lagrange’s equation of motion in a space.

13) Examination of canonical transformation.

14) Determination of Poisson’s bracket.

15)Determination of surface equation of Helicoid.

16) Determination of surface equation of Cone.

**DSE-2 (Number Theory)**

**Unit I:**

Divisibility Theory in the Integers and Congruences: Number Theory, The Division Algorithm, The Greatest Common Divisor, The Euclidean Algorithm, The Diophantine Equation ax + by = c. The Fundamental Theorem of Arithmetic. Basic Properties of Congruence, Binary and Decimal Representations of Integers, Linear Congruences and the Chinese Remainder Theorem.

**Unit II:**

Fermat's Theorem and its Euler’s Generalizations: Pierre de Fermat, Fermat's Little Theorem and Pseudoprimes, Wilson's Theorem, The Fermat-Kraitchik Factorization Method. Euler's Phi-Function, Euler's Theorem, Some Properties of the Phi-Function.

**Unit III:**

Number-Theoretic Functions: The Sum and Number of Divisors, The Möbius Inversion Formula, The Greatest Integer Function, An Application to the Calendar.

**Unit IV:**

Primitive Roots and The Quadratic Reciprocity: The Order of an Integer Modulo n, Primitive Roots for Primes, Composite Numbers Having Primitive Roots, Theory of Indices. Euler's Criterion, The Legendre Symbol and Its properties, Quadratic Reciprocity, Quadratic Congruences with Composite Moduli.

**Text Book:**

1.David Burton, Elementary Number Theory.

**Reference Books:**

1. Niven and Zuckerman, An introduction to the Theory of Numbers, Wiley Publishers.

2. K. Ireland and M. Rosen, A Classical Introduction to Modern Number Theory (Second Edition, Springer)

**Semester-III**

**Paper – XI (Code: 3T1)**

**Complex Analysis**

**Unit I:** Impossibility of ordering Complex numbers. Extended complex plane and stereographic projection. Elementary properties and examples of analytic Functions: Power series, analytic functions.

**Unit II:**Analytic functions as mappings, Mobius transformations. Power series representation of analytic functions, zeros of an analytic function, index of a closed curve.

**Unit III:**Cauchy’s theorem and integral formula, the homotopic version of cauchy’s theorem and simple connectivity, counting zeros; the open mapping theorem, Goursat’s theorem, Classification of singularities, residues, the argument principle.

**Unit IV:**The maximum principle. Schwarz’s lemma. convex functions and Hadamards three circles theorem. Phragmen-Lindel of theorem.

**Text Book**:

Functions of one complex variable: John B. Conway, Second edition, Springer international Student Edition.

**Reference Book:**

Complex Analysis, L.V. Ahlfors. Mc-Graw Hill, 1966.

**Paper – XII (Code: 3T2)**

**Functional Analysis**

**Unit I:** Normed spaces, Banach spaces, Further properties of normed spaces. Finite dimensional normed spaces and subspaces. Compactness and finite dimension. Bounded and continuous linear operators.

**Unit II:** Linear functionals. Normed spaces of operators. Dual spaces. Inner product space. Hilbert space. Further properties of inner product spaces. Orthogonal complements and direct sums. Orthonormal sets and sequences. Total orthonormal sets and sequences.

**Unit III:** Representation of functionals on Hilbert spaces. Hilbert adjoint operators, self-adjoint, unitary and normal operators. Hahn-Banach Theorem, Hahn-Banach Theorem for complex vector spaces and normed spaces. Reflexive spaces.

**Unit IV:** Category theorem, Uniform boundedness theorem, strong and weak convergence, Convergence of sequences of operators and functionals. Open mapping theorem, Closed linear operators and closed graph theorem.

**Text Book:**

Introductory Functional Analysis with Applications by E. Kreyszig, John Wiley and Sons.

**Reference Books:**

1. Introduction to Functional Analysis by A.E. Taylor and D.C. Lay, John Wiley and Sons.

2. Introduction to Topology and Modern Analysis: G.F. Simmons, Mc Graw Hill

**Paper – XIII (Code: 3T3)**

**Mathematical Methods**

**Unit I:**Fourier integral theorem. Fourier transform. Fourier cosine and sine transform. The convolution integral. Multiple Fourier transform. Solution of partial differential equation by means of Fourier transform.

**Unit II:**Calculations of the Laplace transform of some elementary functions. Laplace transforms of derivatives. The convolution of two functions. Inverse formula for the Laplace transform. Solutions of ordinary differential equations by Laplace transform.

**Unit III:**Finite Fourier transform. Finite Sturm-Liouville transforms. Generalized finite Fourier transform.

**Unit IV:**Finite Hankel transform. Finite Legendre transform. Finite Mellin transform.

**Text Book:**

The use of integral transforms: I N. Sneddon, Tata Mc Graw Hill Publishing Company Ltd.

**References Books:**

Modern Mathematics For Engineers: Edwin F Beckenbach, Second series, Mc Graw Hill Book Company

**Core Elective**

**Paper – XIV (Code: 3T4)**

**Fluid Dynamics-I**

**Unit I:** Real fluids and ideal fluids. Velocity of a fluid at a point. Stream lines and path lines. Steady and unsteady flows. Velocity potential. Velocity vector. Local and particle rate of change. Equation of continuity. Acceleration of a fluid. Condition at a rigid boundary. General analysis of fluid motion. Euler’s equation of motion. Bernoulli’s equation. Worked examples. Discussion of the case of steady motion under conservative body forces. Some further aspects of vortex motion.

**Unit II:** Sources, sinks and doublets. Images in a rigid infinite plane. Images in solid spheres. Axisymmetric flows. Stokes’ stream function. The complex potential for twodimensional irrotational,incompressible flow. Complex velocity potential for standard two-dimensional flow. Uniform stream. Line source and line sink. Line doublets. Line vortices. Two-dimensional image systems. The Milne-Thomson circle theorem. Circle Theorem. Some applications of circle theorem. Extension of circle theorem. The theorem of Blasius.

**Unit III:**The equations of state of a substance, the first law of thermodynamics, internal energy of a gas, functions of state, entropy, Maxwell’s thermodynamic relation, Isothermal Adiabatic and Isentropic processes. Compressibility effects in real fluids, the elements of wave motion. One dimensional wave equation, wave equation in two and three dimensions, spherical waves, progressive and stationary waves.

**Unit IV**:The speed of sound in a gas, equation of motion of a gas. Sonic, subsonic, supersonic flows; isentropic gas flow. Reservoir discharge through a channel of varying section, investigation of maximum mass flow through a nozzle, shock waves, formation of shock waves, elementary analysis of normal shock waves.

**Text Book:**

F. Chorlton, Text book of Fluid Dynamics, CBS Publishers, Delhi 1985.

**Reference Books:**

1. G.K. Batchelor, An Introduction to fluid Mechanics, Foundation Books, New Delhi 1994.

2. M.D. Raisinghania, fluid Mechanics, S. Chand and Company, Delhi

**CORE SUBJECT CENTRIC (Only Students of Mathematics)**

**Paper – XIV (Code: 3T5)**

**Operations Research–I**

**Unit I:** Operations Research: Origin, Definition and scope. Linear Programming: Formulation and solution of linear programming problems by graphical and simplex methods, Big - M and two-phase methods, Degeneracy, Duality in linear programming.

**Unit II:**Transportation Problems: Basic feasible solutions, Optimum solution by stepping stone andmodified distribution methods, Unbalanced and degenerate problems, Transhipment problem.Assignment problems: Hungarian method, Unbalanced problem, Case of maximization, Travelling salesman and crew assignment problems.

**Unit III:**Concepts of stochastic processes, Poisson process, Birth-death process, Queuing models: Basic components of a queuing system, Steady-state solution of Markovian queuing models with single and multiple servers (M/M/1. M/M/C, M/M/1/k, M/MC/k ).

**Unit IV:**Inventory control models: Economic order quantity (EOQ) model with uniform demand, EOQ when shortages are allowed, EOQ with uniform replenishment, Inventory control with price breaks.

**Text book:** Operations Research: Kanti Swarup P.K. Gupta and Man Mohan: Sultan Chand and Sons New Delhi.

**Refference Books**:

1. H. A. Taha, Operations Research – An Introduction, Prentice-Hall, 1997.

2. J. K. Sharma, Operations Research: Theory and Applications, Macmillan, 1997

3. S. D. Sharma, H. Sharma, Operations Research: Theory, Methods and Applications, Kedar Nath Ram Nath, 1972

4. S. S. Rao, Optimization-Theory and Applications, Wiley Eastern Ltd., 1977.

5. F. S. Hillier, G. J. Lieberman, Introduction to Operations Research, McGraw-Hill, 2001

6. M. S. Bazaraa, H. D. Sherali, C. M. Shetty, Nonlinear Programming-Theory and Algorithms, Wiley-Interscience, 2006

7. A. K. Bhunia and L. Sahoo, Advanced Operations Research, Asian Books Private Limited, New Delhi, 2011.

8. M. Aokie, Introduction to Optimization Techniques: Fundamentals and Applications of Nonlinear Programming, The Macmillan Company, 1971

**Semester-IV**

**Paper – XVI (Code: 4T1)**

**Dynamical Systems**

**Unit I:**Dynamical systems and vector fields. The fundamental theorem. Existence and uniqueness. Continuity of solutions in initial conditions. On extending solutions. Global solutions. The flow of a differential equation.

**Unit II:**Nonlinear sinks. Stability. Liapunov function. Gradient systems. Gradients and inner products.

**Unit III:**Limit sets, local sections and flow boxes, monotone sequences in planar dynamical systems. The Poincare Bendixson theorem, Applications of Poincare Bendixson theorem; one species, predator and prey, competing species.

**Unit IV:**Asymptotic stability of closed orbits, discrete dynamical systems. Stability and closed orbits. Non autonomous equations and differentiability of flows. Persistence of equilibria, persistence of closed orbits. Structural stability.

**Text Book:**

Differential equations, dynamical systems & linear algebra: M.W. Hirsch & S. Smale, Academic Press, 1975.

**Reference Book:**

Dynamical systems: V.I. Arnold, Springer Verlag, 1992.

**Paper – XVII (Code: 4T2)**

**Partial Differential Equations**

**Unit I:** Curves and surfaces, First order Partial Differential Equations, classification of first order partial differential equations, classifications of Integrals, Linear equations of first order. Pfaffian differential equations, Criteria of Integrability of a Pfaffian differential equation. Compatible systems of first order partial differential equations.

**Unit II:**Charpits method, Jacobi method of solving partial differential equations, Integral surfaces through a given curve for a linear partial differential equation: Cauchy Problem, Quasi Linear Equations: Geometry of Solutions, Non-linear First Order partial differential equations.

**Unit III:** Second order Partial Differential Equations, Classification of second order partial differential equation, Vibration of an infinite string (both ends are not fixed), Physical Meaning of the solution of the wave equation. Vibration of a semi-infinite string, Vibration of a string of finite length:(Method of separation of variables), Uniqueness of solution of wave equation. Heat conduction Problems with finite rod and infinite rod.

**Unit IV:** Laplace equation, Boundary Value Problems: Dirichlet’s problems and Neumann problems, Maximum and minimum principles. Dirichlet Problems and Neumann problems for a circle, for a rectangle and for a upper half plane, Families to equipotential surfaces, Solution of Laplace equation, Laplace equation in polar form, Laplace equation in spherical polar coordinates. Kelvin’s inversion theorem, Stability theorem, Duhamel's Principle.

**Text Book:**

1. T. Amarnath: An elementary course in Partial differential equations, 2nd edition, Narosa

publishing House (2012).

**Reference Books:**

1. Mark Pinsky: Partial differential equations and boundary-value problems with applications, AMS,3rd edition (2011).

2. I. N. Sneddon: Elements of Partial Differential Equations, McGraw Hill Int.

3. Fritz John: Partial Differential Equations, Springer(1952).

**Paper – XVIII (Code: 4T3)**

**Advanced Numerical Methods**

**Unit I:**Simple enclosure methods, Secant method, Newton’s method, general theory for one point iteration methods. Aitken extrapolation for linearly convergent sequences, Error tests, Numerical evaluation of multiple roots, roots of polynomials, Mullers method, Non-linear systems of equations, Newton’s method for non- linear systems.

**Unit II:**Polynomial interpolation theory, Newton’s divided differences, finite difference and table-oriented interpolation formulas. Forward-differences. Hermite interpolation.

**Unit III**: The Weierstrass theorem and Taylor’s theorem. The minimax approximation problem, the least square approximation problem, orthogonal polynomial, economisation of Taylor series, minimax approximation.

**Unit IV:** The trapezoidal rule and Simpson’s rule, Newton- Cotes integration formulas.

**Text book:**

An Introduction to Numerical Analysis by K. E. Atkinson, Johan Wiley and sons, Inc.

**Core Elective**

**Paper – XIX (Code: 4T4)**

**Fluid Dynamics-II**

**Unit I:** Stress components in a real fluid, relation between Cartesian components of stress translation motion of fluid elements, the rate of strain quadric and principal stresses, some further properties of the rate of the strain quadric, stress analysis in fluid motion, relation between stress and rate of strain, the coefficient of viscosity and laminar flow, the Navier-Stokes equations of motion of a viscous fluid, some solvable problems in viscous flow, diffusion of vorticity, energy dissipation due to viscosity, steady flow past a fixed sphere.

**Unit II:**Nature of magneto-hydrodynamics, Maxwell electromagnetic field equations; Motion at rest, Motion in medium, Equation of motion of conducting fluid, Rate of flow of charge, Simplification of electromagnetic field equation. Magnetic Reynold number; Alfven’s theorem, The magnetic body force. Ferraro’s Law of Isorotation.

**Unit III:**Dynamical similarity, Buckingham Theorem. Renold number. Prandtl’s boundary layer, Boundary layer equation in two dimensions, Blasius solutions, Boundary layer thickness, Displacement thickness. Karman integral conditions, Separation of boundary layer flow.

**Unit IV:**Turbulence: Definition of turbulence and introductory concepts. Equations of motion for turbulent flow. Reynolds Stresses Cylindrical coordinates. Equation for the conservation of a transferable scalar quantity in a turbulent flow. Double correlations between turbulence-velocity components. Change in double velocity correlation with time. Introduction to triple velocity correlations. Features of the double longitudinal and lateral correlations in a homogeneous turbulence. Integral scale of turbulence.

**Text Books**:

1. Text book of Fluid Dynamics: F. Chorlton; CBS Publishers, Delhi 1985.

2. Fluid Mechanics: Joseph Spurk; Springer.

3. Turbulence by J.O. Hinze, 2nd edition, Mc Graw-Hill, chapter 1 sections 1.1 to 1.7

4. Fluid Mechanics by M.D. Raisinghania, S. Chand and Company, Delhi.

**Reference Books:**

1. An Introduction to fluid Mechanics: G.K. Batchelor; Foundation Books, New Delhi, 1994.

2. Boundary Layer Theory: H. Schichting; Mc Graw Hill Boo

**CORE SUBJECT CENTRIC (Only Students of Mathematics)**

**Paper – XX (Code: 4T5)**

**Operations Research–II**

**Unit I:** Revised simplex method (with and without artificial variables). Post Optimality Analysis: changes in (i) objective function, (ii) requirement vector, (iii) coefficient matrix; Addition and deletion of variables, Addition of constraints.

**Unit II:**Integer Programming: Gomory’s cutting plane algorithm (All integer and mixed integer algorithms), Branch and Bound method.

**Unit III:**Bounded variable technique for L.P.P. Unconstrained optimization, Constrained optimization with equality constraints- Lagrange’s multiplier method, Interpretation of Lagrange multiplier.

**Unit IV:**Inventory control: Deterministic inventory models including price breaks. Multi-item inventory model with constraints. Queueing Theory: Basic features of queueing systems, operating characteristics of a queueing system, arrival and departure (birth & death) distributions, inter-arrival and service times distributions, transient, steady state conditions in queueing process. Poisson queueing models- M/M/1, M/M/C for finite and infinite queue length.

**Text book:**

Operations Research: Kanti Swarup P.K. Gupta and Man Mohan: Sultan Chand and Sons New Delhi.

**Reference Books:**

1. H. A. Taha, Operations Research – An Introduction, Prentice-Hall, 1997.

2. J. K. Sharma, Operations Research: Theory and Applications, Macmillan, 1997

3. S. D. Sharma, H. Sharma, Operations Research: Theory, Methods and Applications, Kedar Nath Ram Nath, 1972

4. S. S. Rao, Optimization-Theory and Applications, Wiley Eastern Ltd., 1977.

5. F. S. Hillier, G. J. Lieberman, Introduction to Operations Research, McGraw-Hill, 2001

6. M. S. Bazaraa, H. D. Sherali, C. M. Shetty, Nonlinear Programming-Theory and Algorithms, Wiley-Interscience, 2006

7. A. K. Bhunia and L. Sahoo, Advanced Operations Research, Asian Books Private Limited, New Delhi, 2011.

8. M. Aokie, Introduction to Optimization Techniques: Fundamentals and Applications of Nonlinear Programming, The Macmillan Company, 1971.